



Consiglio Nazionale  
delle Ricerche

# STS-EPR

A mechanistic approach for modelling spatial, temporal and social aspects of human mobility

Author: Giuliano Cornacchia

09-04-2021

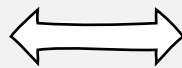
# Introduction

- **Human mobility** is the discipline that studies the movements of individuals in **space** and **time**.
- The increase of GPS devices and location-based services allows to collect **digital footprints** of human's movements.

Trajectory



Definition

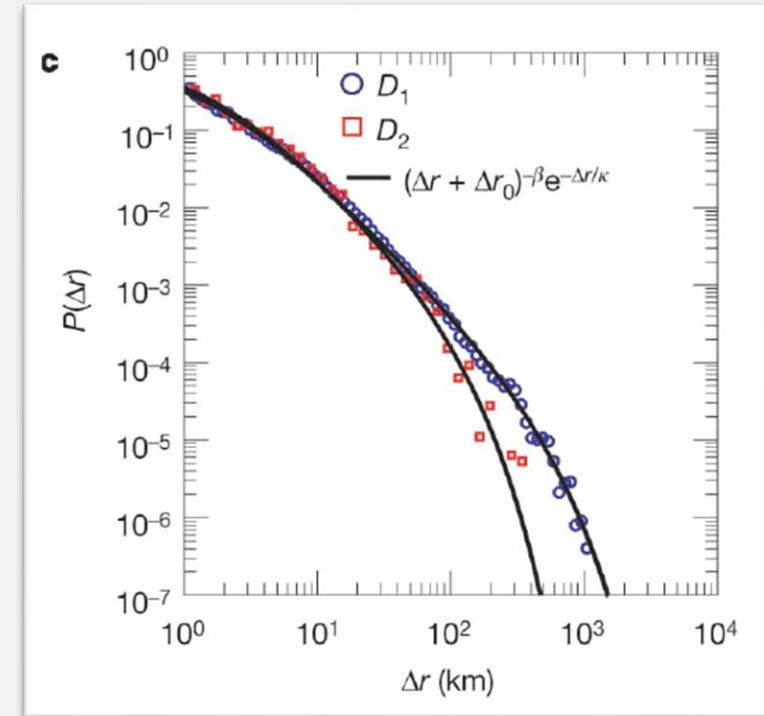


$$T = \langle (r_0, t_0), (r_1, t_1), \dots, (r_n, t_n) \rangle$$



# Introduction

- The large availability of digital traces of our displacements, offers the possibility to study human movements at a **large scale** and in **detail**.
- Several mobility patterns emerge [1, 2]:
  - **Power-law** behavior of  $\Delta r$ ,  $r_g$ , and  $\Delta t$
  - Tendency to **return** to few location visited before
  - Move at **specific times** of the day



[1] Brockmann, D., Hufnagel, L., Geisel, T., 2006. The scaling laws of human travel. Nature 439, 462–5.

[2] Gonzalez, M.C., Hidalgo, C., Barabasi, A.L., 2008. Understanding individual human mobility patterns. Nature 453, 779–82.

# Introduction

- Mobility trajectory data are of **fundamental** importance in different disciplines [3]:



Epidemic modeling



Traffic optimization



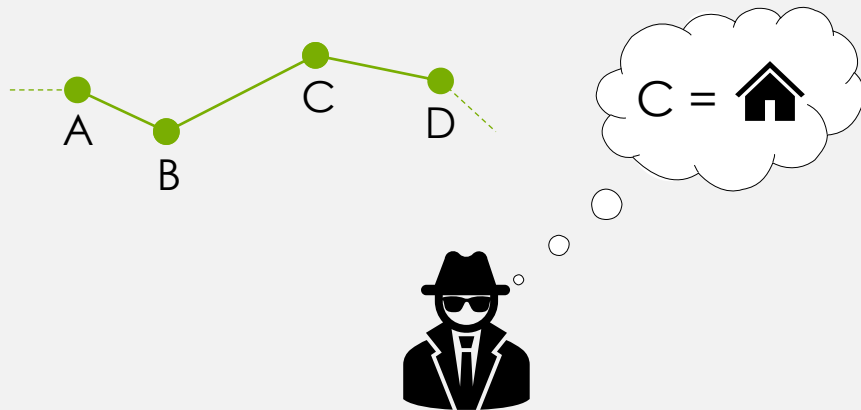
What-if analysis

[3] Barbosa-Filho et al. 2018. Human mobility: Models and applications.

# Introduction

## Problem

- Mobility trajectory data are sensitive: they suffer from **privacy attacks** [4]

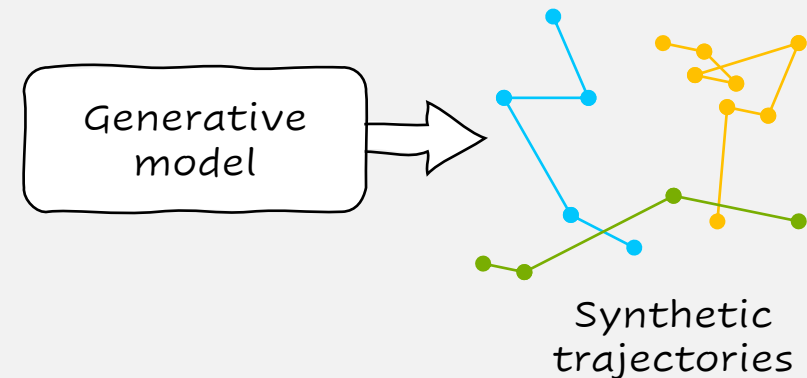


- Companies **cannot** make mobility data freely available

[4] Montjoye, Y.A., Hidalgo, C., Verleysen, M., Blondel, V., 2013. Unique in the crowd: The privacy bounds of human mobility. Scientific reports 3, 1376.

## Solution

- **Generative models**
  - Generate **synthetic** yet **realistic** trajectories
  - **Reduce** the cost of the data collection phase (time and money)
  - Produce trajectories for new scenarios

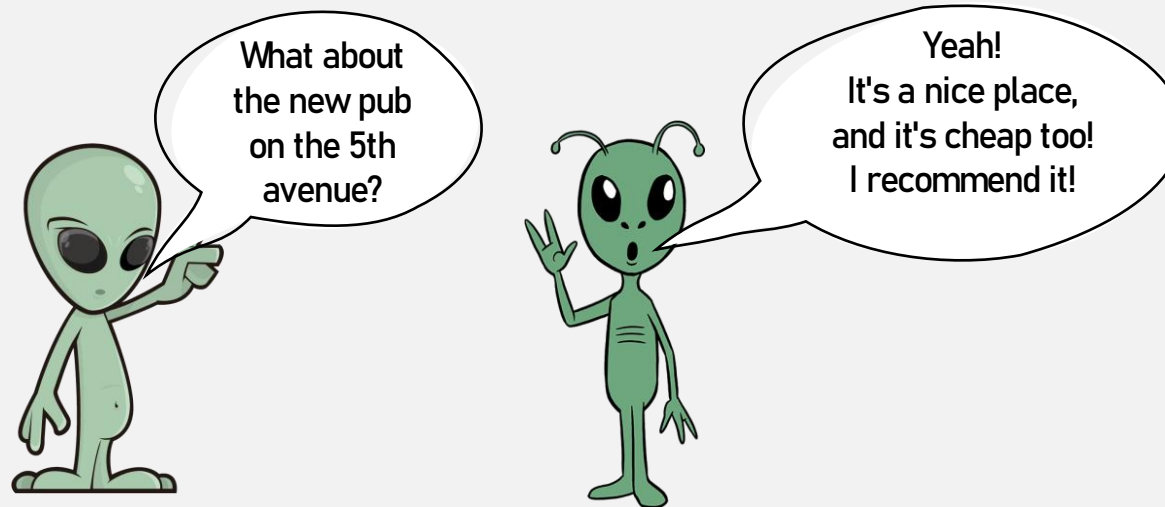


# Introduction

- A mechanistic model assumes that a complex system can be understood by examining the workings of its individual parts and the way they are coupled.
- They use **pre-calculated statistical functions** based on prior knowledge of human mobility.
- **PROS**
  - + Explainability
  - + Transferability
- **CONS**
  - Cannot capture all the aspects of mobility

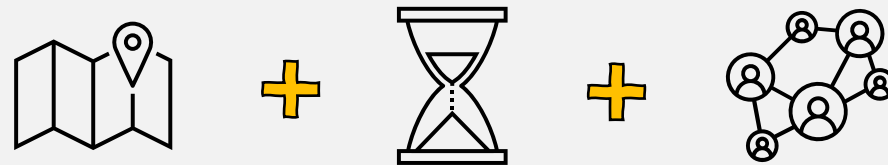
# Introduction

- Most of the generative models focus only on the **spatial** and **temporal** dimensions of mobility.
- What about the **social** dimension?
  - $\approx$  **30%** of an individual's movements are taken for **social** purposes [8].
  - Individuals are more likely to visit a location if it has been **recommended** by a friend.



# STS-EPR

- STS-EPR (Spatial, Temporal, and Social EPR) is a **mechanistic** generative model that embeds mechanisms to capture the **spatial**, **temporal** and **social** aspects of mobility together.



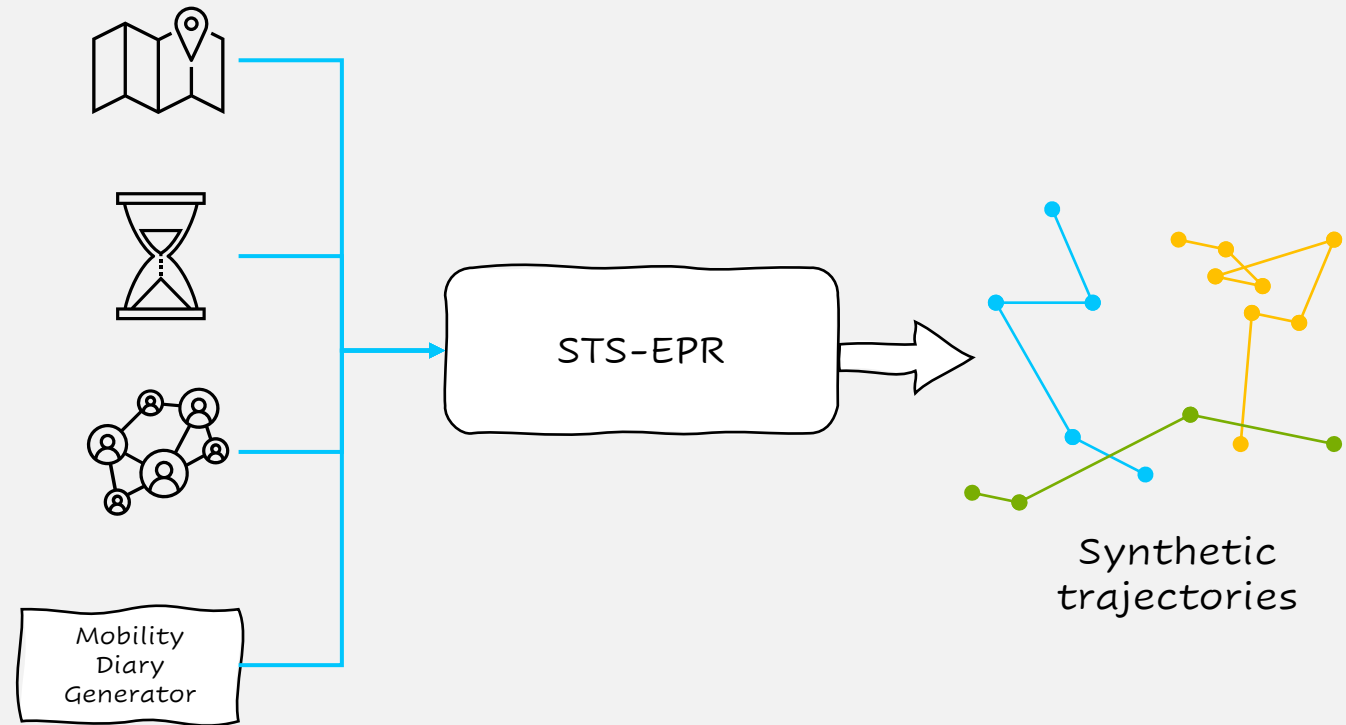
- STS-EPR couples the advantages of two state-of-the-art generative models:
  - **GeoSim [5]**: it considers the social dimension, but its spatial and temporal realism is limited.
  - **DITRAS [6]**: it is able to capture the individual's circadian rhythm using a **Mobility Diary Generator (MDG)**, as well as the spatial aspects of mobility, but it does not take into account the sociality of individuals.

[5] Toole, J., Herrera-Yague, C., Schneider, C., Gonzalez, M.C., 2015. Coupling human mobility and social ties. *Journal of the Royal Society*.

[6] Pappalardo, L., Simini, F., 2017. Data-driven generation of spatio-temporal routines in human mobility. *Data Mining and Knowledge Discovery*, 32.

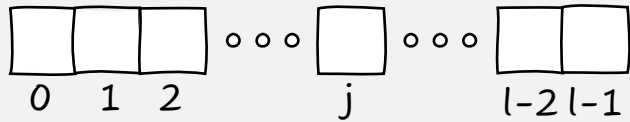


# STS-EPR

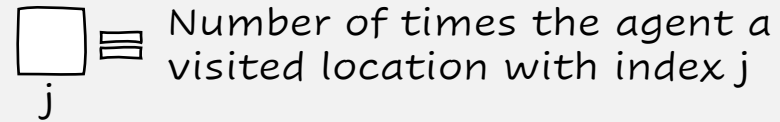


# STS-EPR

- Location Vector [5]



Location vector ( $lva$ )

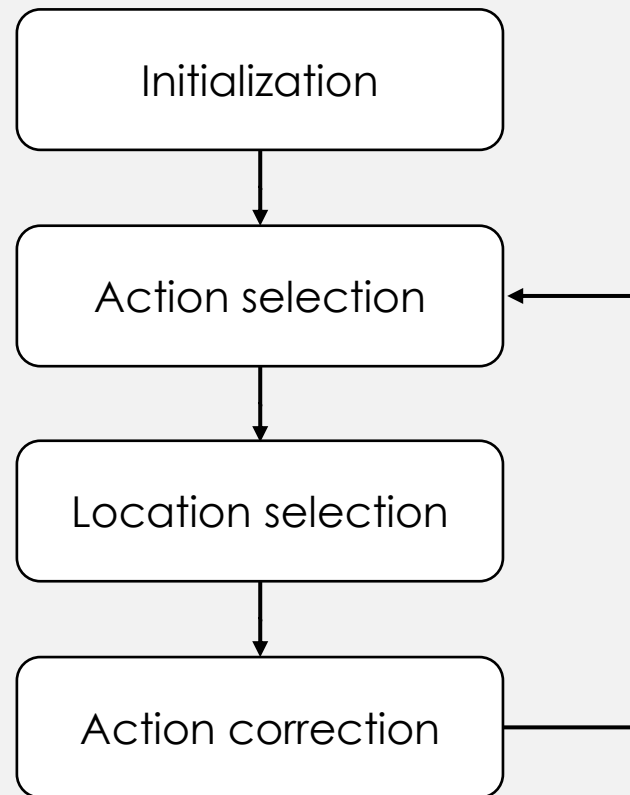


- Mobility Similarity [5]

- The **mobility similarity** ( $mob_{sim}$ ) between two agents is defined as the **cosine similarity** of their **location vectors**.

# STS-EPR

- STS-EPR is composed of **four** phases:

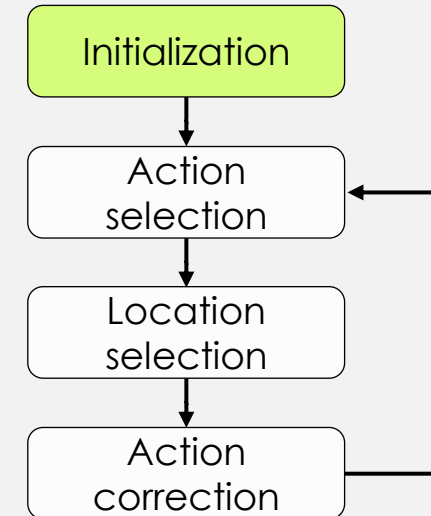
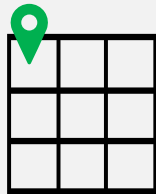


# STS-EPR: Initialization phase

- The  $N$  synthetic individuals are connected in an undirected graph  $G$ . Each edge's **weight** represents the **mobility similarity** of the linked agents.
- The model assigns at each agent a **mobility diary** produced by the MDG.

$\langle (ab_0, t_0), (ab_1, t_1), \dots, (ab_0, t_j) \dots \rangle$

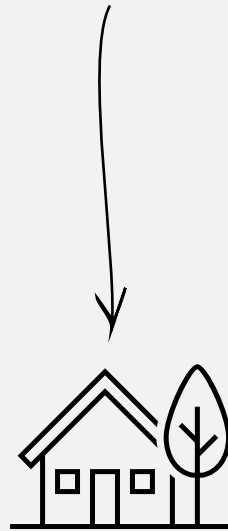
- The agents are assigned to a starting location  $i$  with a probability  $p(i) \propto w_i$ , where  $w_i$  is the **relevance** of location  $i$ .



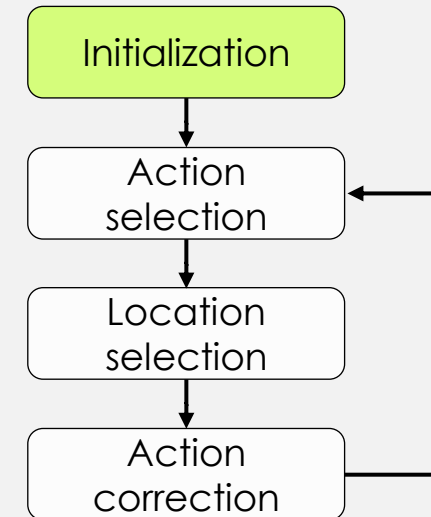
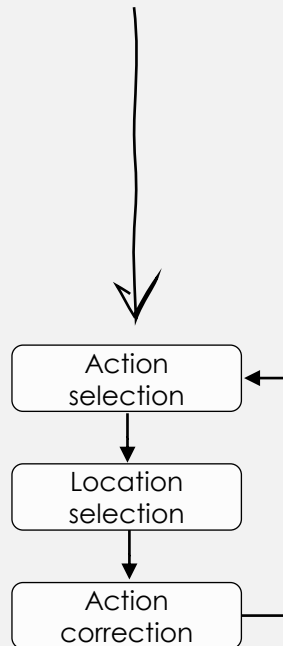
# STS-EPR: Initialization phase

- Each agent moves according to its mobility diary's entries at the time specified.

$(ab_0, t_k)$



$(ab_i, t_k)$   
 $i > 0$



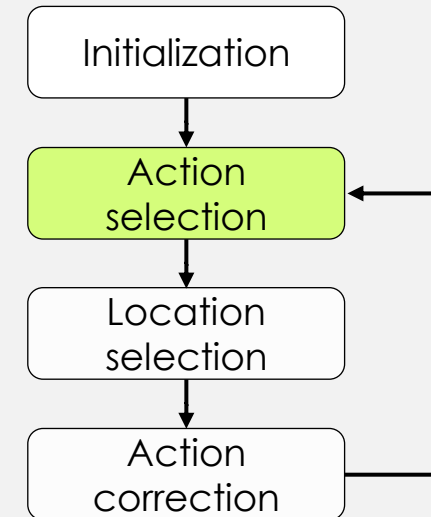
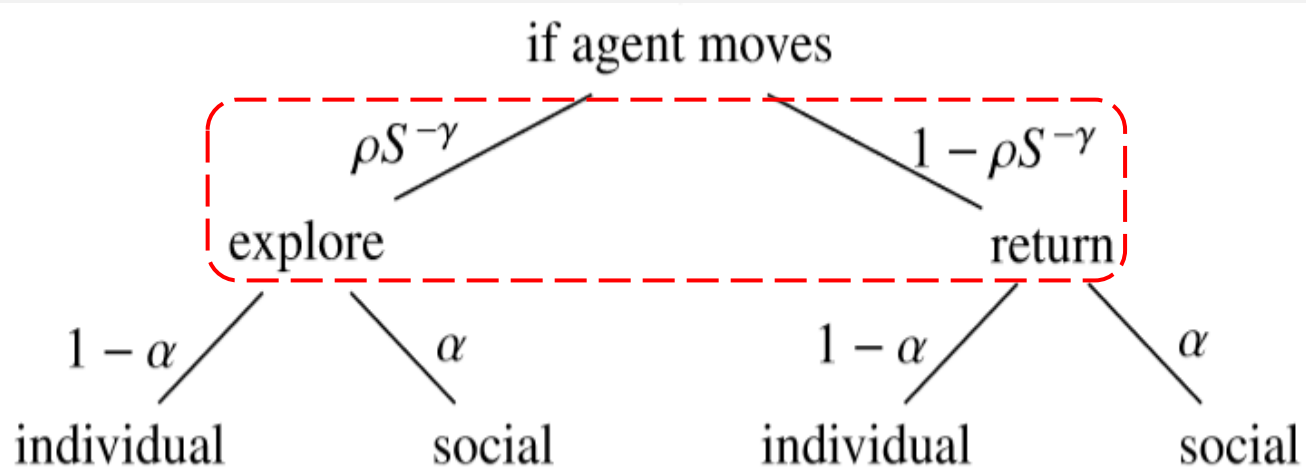
# STS-EPR: Action Selection phase

- In this phase the agent selects with **which mechanisms** to move.
- First, the agent selects between two competing **spatial** mechanisms: **exploration** and **preferential return**.

$$\rho = 0.6$$

$$\gamma = 0.21$$

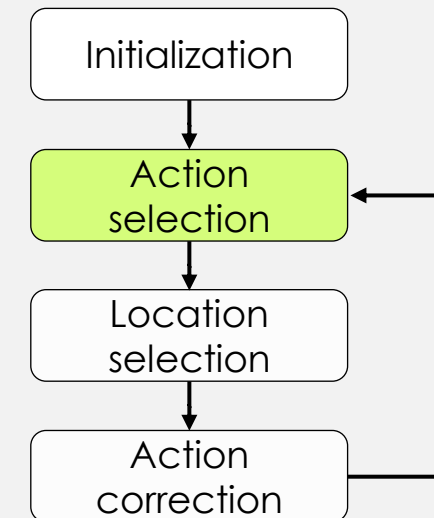
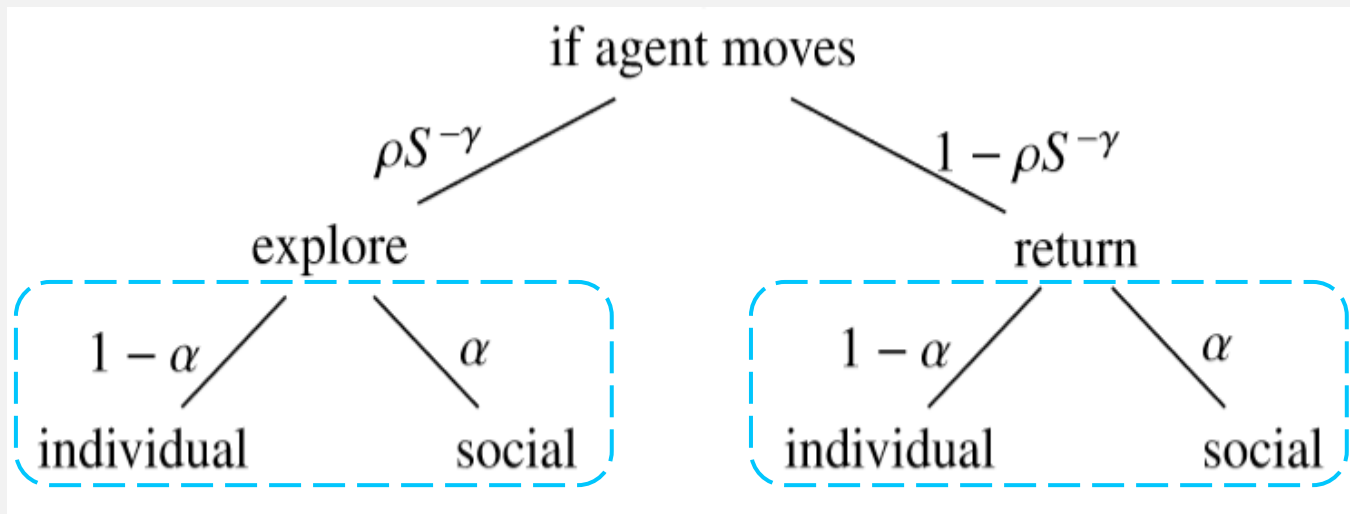
$S$  = number of unique visited locations



# STS-EPR: Action Selection phase

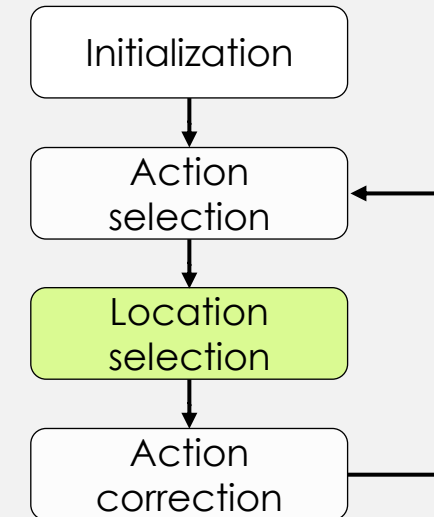
- Then, the agent selects between two competing **social** mechanisms: **individual** and **social influence**.

$$\alpha = 0.2$$



# STS-EPR: Location Selection phase

- During the location selection phase, the agent decides **which location** will be the **destination** of its next displacement, according to the combinations of the **spatial** and **social** mechanisms picked.
- There are **four** possible combinations:
  1. **Individual** – **Exploration**
  2. **Individual** – **Return**
  3. **Social** – **Exploration**
  4. **Social** – **Return**





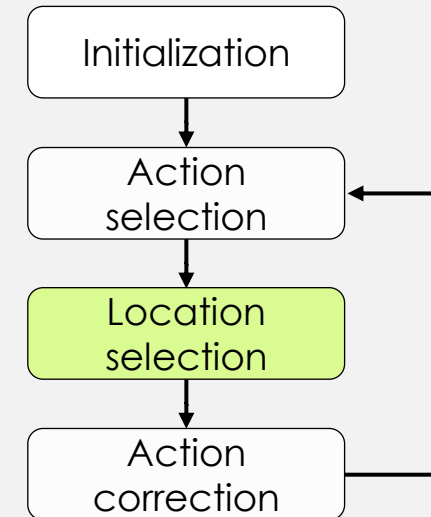
# STS-EPR: Location Selection phase

## Individual – Exploration:

- The agent selects to visit an **unvisited** location **without the influence** of its social contacts.
- If the agent is currently at location  $i$  it selects an **unvisited** location  $j$  with probability

$$p(j) \propto \frac{w_i w_j}{d_{ij}^2}$$

- $d_{ij}$  is the distance between locations  $i$  and  $j$ .
- The relevance of a location  $k$  is  $w_k$ .



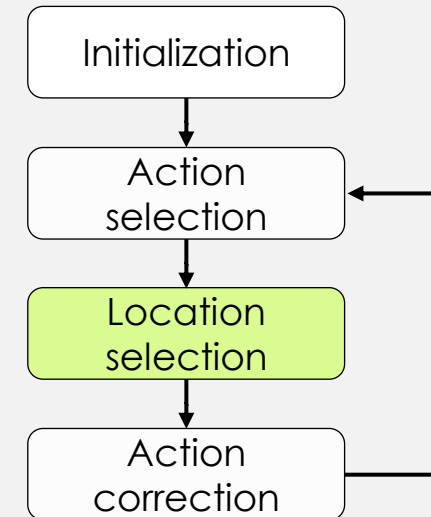
# STS-EPR: Location Selection phase

## Individual – Return:

- The agent selects to **return** to a **visited** location **without the influence** of its social contacts.
- The agent, currently at location  $i$ , decides to return to location  $j$  with probability

$$p(j) \propto f_a(j)$$

- Where  $f_a(j)$  is defined as:  $\frac{lv_a[j]}{\sum_{j=1}^{|L|} lv_a[i]}$



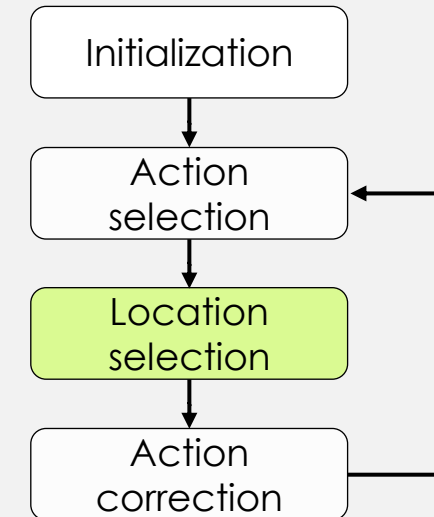
# STS-EPR: Location Selection phase

## Social – {Exploration, Return}:

- The agent selects a **visited** (**Return**) or **unvisited** (**Exploration**) location to return **with the influence** of its social contacts.
- The agent  $a$  selects a **social contact**; the probability of a social contact  $c$  to be selected is

$$p(c) \propto mob_{sim}(a, c)$$

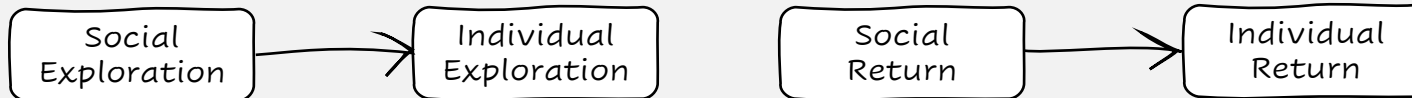
- After the social contact  $c$  is selected, the agent  $a$  selects **the proper location**  $i$ , according to the spatial mechanism picked, with probability  $p(i) \propto f_c(i)$



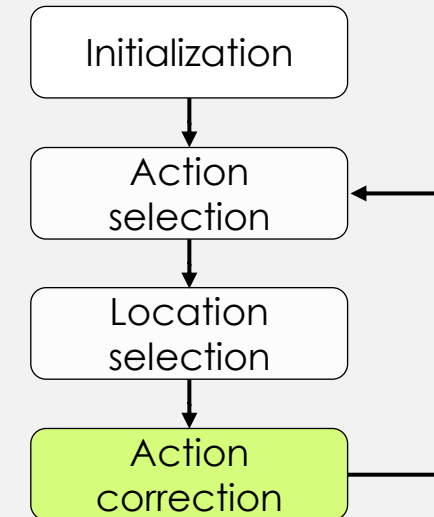
# STS-EPR: Action Correction phase

The set of possible locations an agent can reach **is limited**.

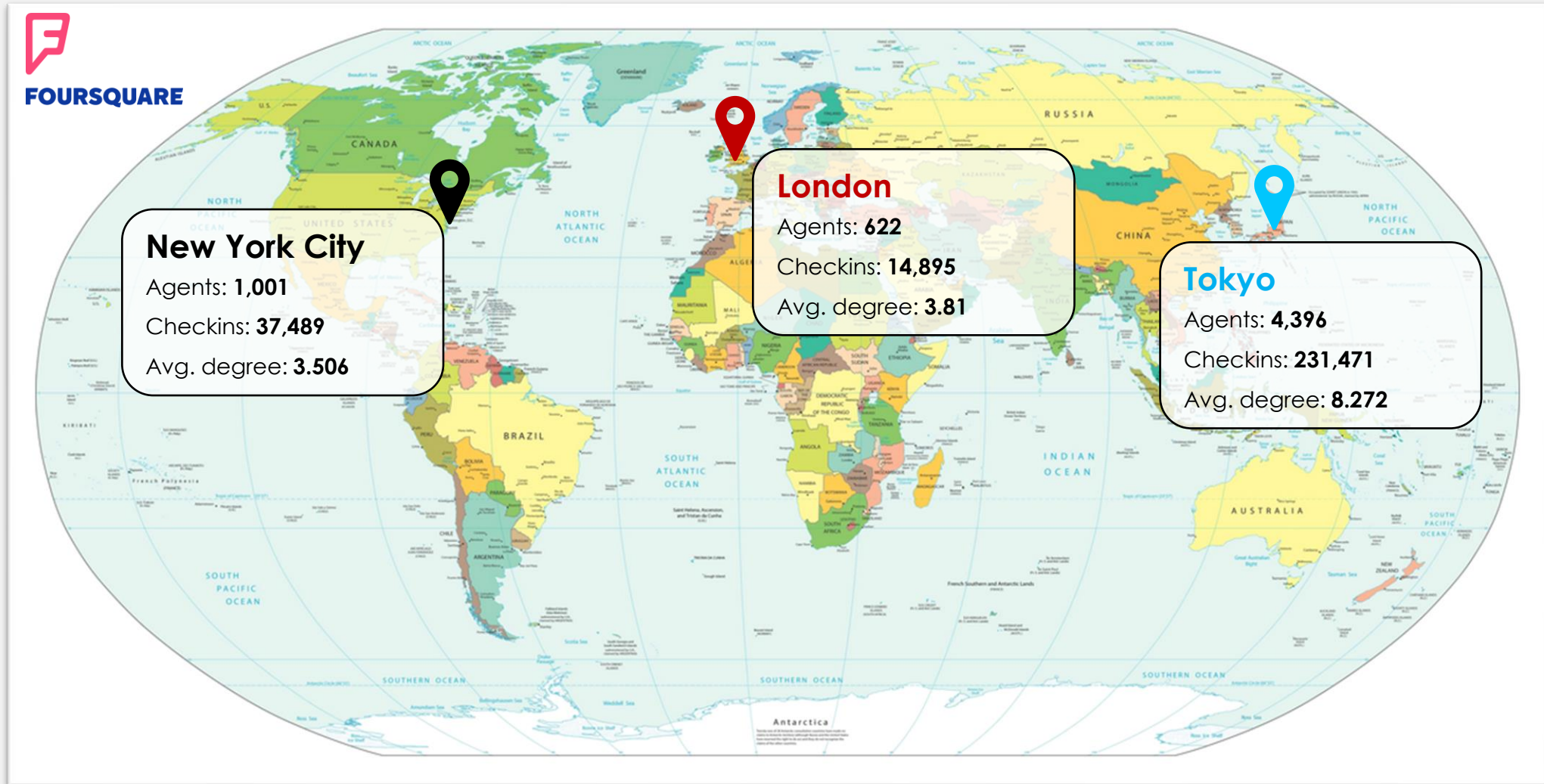
- **No location in social choices:** if no location visited by a social contact  $c$  is feasible for the agent  $a$ , the action is corrected from **Social** – {Exploration, Return} to **Individual** – {Exploration, Return}



- **No new location to explore:** when an agent decides to explore but it visited all the locations at least once we force the agent to make an **Individual** – **Return**.

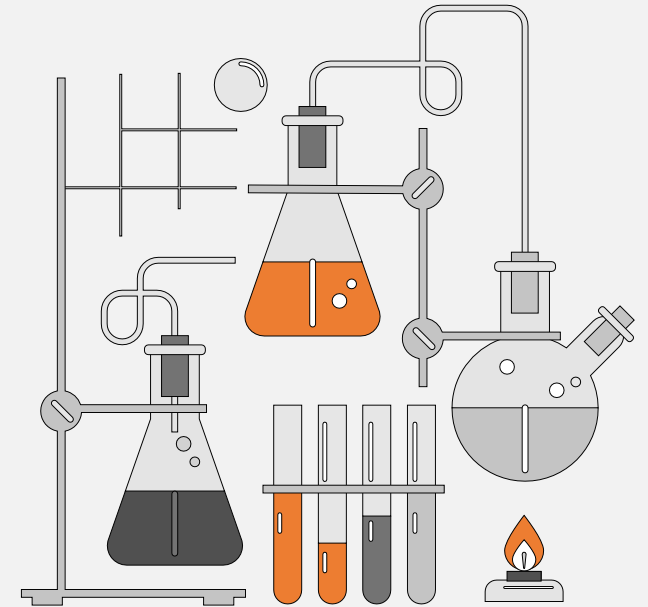


# Experiments



# Experiments

- We validate **STS-EPR** using as baselines **DITRAS** and **GeoSim**.
- For each city, we **compare** the **synthetic** trajectories with **real** ones extracted from Foursquare's checkins [7].
- The similarity between the two sets of trajectories is computed with respect to the mobility patterns that characterize human mobility, and it is quantified with the **Kullback-Leibler divergence**.

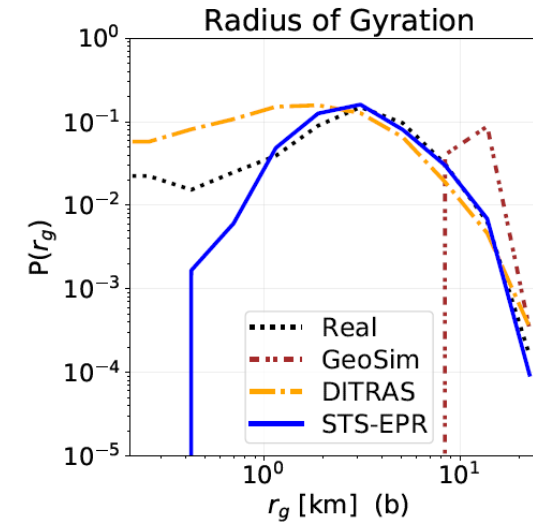
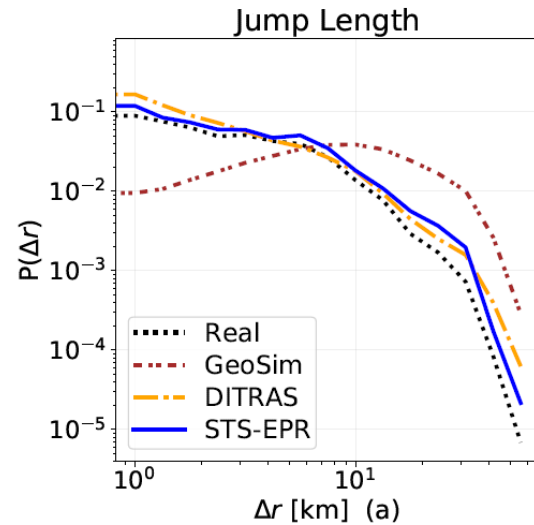


# Results

	Model	$\Delta r$	$r_g$	$f(r_i)$	$VI$	$\Delta_t$	$t(h)$	$E_{unc}$	$mob_{sim}$
London	GeoSim	0.5036 $\pm 0.0075$	4.9381 $\pm 0.0932$	<b>0.0016</b> <b><math>\pm 0.0001</math></b>	4.427 $\pm 0.0069$	0.1962 $\pm 0.0043$	0.281 $\pm 0.0003$	8.5182 $\pm 0.0003$	0.6097 $\pm 0.0079$
	DITRAS	0.0221 $\pm 0.0022$	<b>0.1813</b> <b><math>\pm 0.0239</math></b>	0.1094 $\pm 0.0$	0.1428 $\pm 0.006$	0.166 $\pm 0.0031$	0.0119 $\pm 0.0004$	3.8816 $\pm 0.1897$	0.4347 $\pm 0.0516$
	STS-EPR	<b>0.0108</b> <b><math>\pm 0.0016</math></b>	0.4609 $\pm 0.233$	0.0097 $\pm 0.0003$	<b>0.1032</b> <b><math>\pm 0.0126</math></b>	<b>0.1626</b> <b><math>\pm 0.0035</math></b>	<b>0.0116</b> <b><math>\pm 0.001</math></b>	<b>2.6749</b> <b><math>\pm 0.1169</math></b>	<b>0.2543</b> <b><math>\pm 0.01</math></b>
Tokyo	GeoSim	0.7257 $\pm 0.002$	4.8165 $\pm 0.0042$	<b>0.0002</b> <b><math>\pm 0.0</math></b>	3.0957 $\pm 0.0148$	0.2354 $\pm 0.0003$	0.2837 $\pm 0.0006$	7.1242 $\pm 0.0593$	0.0931 $\pm 0.0017$
	DITRAS	0.0628 $\pm 0.0025$	<b>0.2417</b> <b><math>\pm 0.0171</math></b>	0.1409 $\pm 0.0$	0.1101 $\pm 0.0048$	0.2007 $\pm 0.003$	<b>0.0074</b> <b><math>\pm 0.0001</math></b>	5.0034 $\pm 0.2708$	0.923 $\pm 0.0375$
	STS-EPR	<b>0.0485</b> <b><math>\pm 0.0013</math></b>	0.2504 $\pm 0.0746$	0.0108 $\pm 0.0002$	<b>0.0226</b> <b><math>\pm 0.0019</math></b>	<b>0.2001</b> <b><math>\pm 0.0024</math></b>	0.0076 $\pm 0.0001$	<b>4.8717</b> <b><math>\pm 0.2247</math></b>	<b>0.014</b> <b><math>\pm 0.0009</math></b>
New York City	GeoSim	0.5947 $\pm 0.0062$	5.3913 $\pm 0.0051$	<b>0.0071</b> <b><math>\pm 0.0004</math></b>	3.6418 $\pm 0.0069$	0.1973 $\pm 0.0004$	0.18 $\pm 0.0005$	8.0483 $\pm 0.0579$	0.5879 $\pm 0.0149$
	DITRAS	<b>0.0091</b> <b><math>\pm 0.0006</math></b>	<b>0.2987</b> <b><math>\pm 0.0359</math></b>	0.193 $\pm 0.0026$	0.1281 $\pm 0.0044$	<b>0.1665</b> <b><math>\pm 0.0032</math></b>	<b>0.0066</b> <b><math>\pm 0.0003</math></b>	<b>4.8881</b> <b><math>\pm 0.0248</math></b>	0.5425 $\pm 0.038$
	STS-EPR	0.0188 $\pm 0.0015$	0.3886 $\pm 0.0284$	0.0318 $\pm 0.0008$	<b>0.0531</b> <b><math>\pm 0.004</math></b>	0.1705 $\pm 0.0047$	0.0071 $\pm 0.0005$	5.028 $\pm 1.1511$	<b>0.3066</b> <b><math>\pm 0.0044</math></b>

# Results

	Model	$\Delta r$	$r_g$
London	GeoSim	0.5036 $\pm 0.0075$	4.9381 $\pm 0.0932$
	DITRAS	0.0221 $\pm 0.0022$	<b>0.1813</b> <b><math>\pm 0.0239</math></b>
	STS-EPR	<b>0.0108</b> <b><math>\pm 0.0016</math></b>	0.4609 $\pm 0.233$
Tokyo	GeoSim	0.7257 $\pm 0.002$	4.8165 $\pm 0.0042$
	DITRAS	0.0628 $\pm 0.0025$	<b>0.2417</b> <b><math>\pm 0.0171</math></b>
	STS-EPR	<b>0.0485</b> <b><math>\pm 0.0013</math></b>	0.2504 $\pm 0.0746$
New York City	GeoSim	0.5947 $\pm 0.0062$	5.3913 $\pm 0.0051$
	DITRAS	<b>0.0091</b> <b><math>\pm 0.0006</math></b>	<b>0.2987</b> <b><math>\pm 0.0359</math></b>
	STS-EPR	0.0188 $\pm 0.0015$	0.3886 $\pm 0.0284$

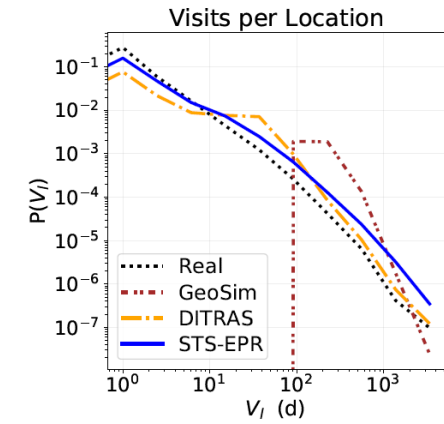
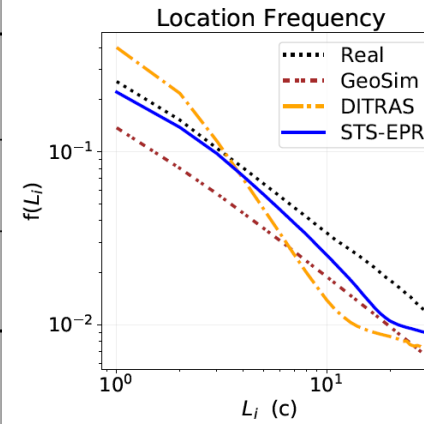


- GeoSim **cannot** reproduce neither  $\Delta r$  nor  $r_g$
- STS-EPR generally better than DITRAS w.r.t.  $\Delta r$
- DITRAS generally better than STS-EPR w.r.t.  $r_g$



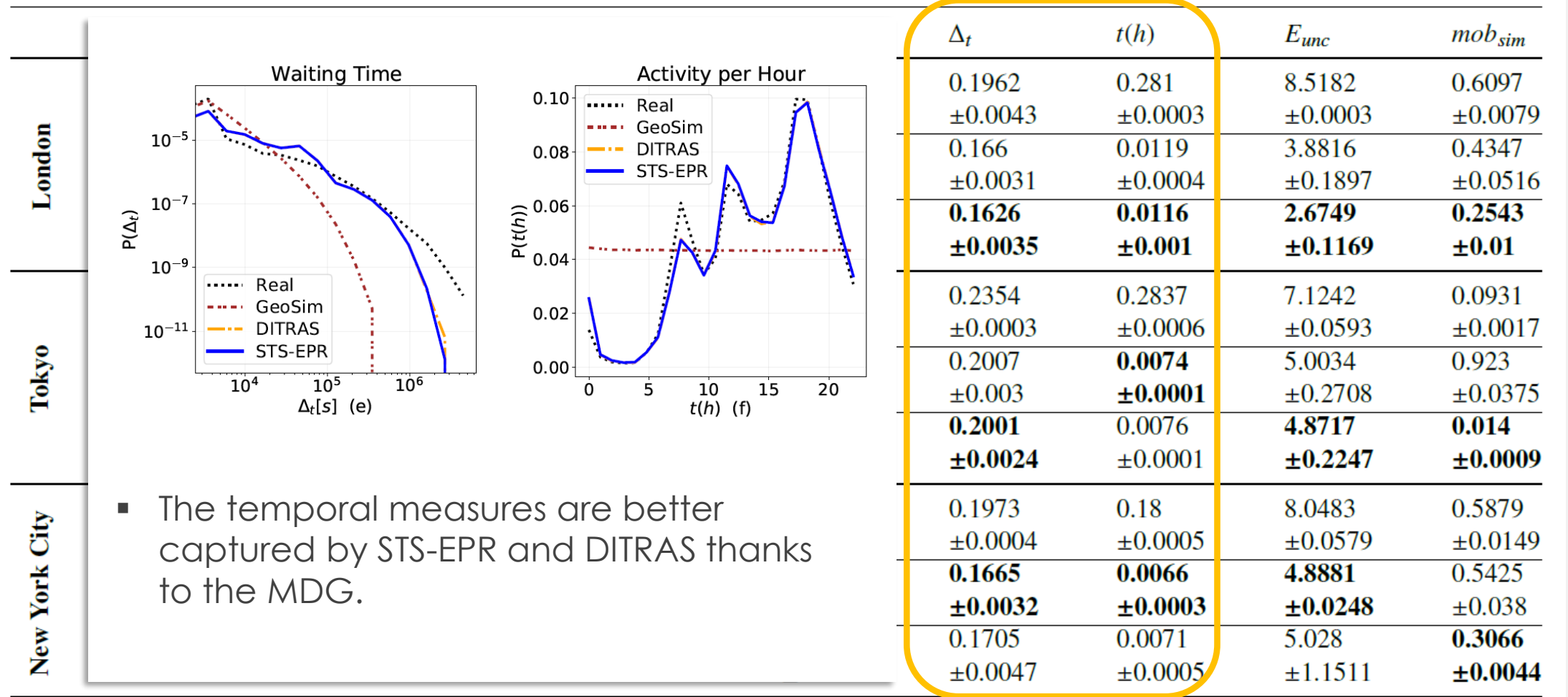
# Results

	Model	$\Delta r$	$r_g$	$f(r_i)$	$V_l$
London	GeoSim	0.5036 $\pm 0.0075$	4.9381 $\pm 0.0932$	<b>0.0016</b> $\pm 0.0001$	4.427 $\pm 0.0069$
	DITRAS	0.0221 $\pm 0.0022$	<b>0.1813</b> $\pm 0.0239$	0.1094 $\pm 0.0$	0.1428 $\pm 0.006$
	STS-EPR	<b>0.0108</b> $\pm 0.0016$	0.4609 $\pm 0.233$	0.0097 $\pm 0.0003$	<b>0.1032</b> $\pm 0.0126$
Tokyo	GeoSim	0.7257 $\pm 0.002$	4.8165 $\pm 0.0042$	<b>0.0002</b> $\pm 0.0$	3.0957 $\pm 0.0148$
	DITRAS	0.0628 $\pm 0.0025$	<b>0.2417</b> $\pm 0.0171$	0.1409 $\pm 0.0$	0.1101 $\pm 0.0048$
	STS-EPR	<b>0.0485</b> $\pm 0.0013$	0.2504 $\pm 0.0746$	0.0108 $\pm 0.0002$	<b>0.0226</b> $\pm 0.0019$
New York City	GeoSim	0.5947 $\pm 0.0062$	5.3913 $\pm 0.0051$	<b>0.0071</b> $\pm 0.0004$	3.6418 $\pm 0.0069$
	DITRAS	<b>0.0091</b> $\pm 0.0006$	<b>0.2987</b> $\pm 0.0359$	0.193 $\pm 0.0026$	0.1281 $\pm 0.0044$
	STS-EPR	0.0188 $\pm 0.0015$	0.3886 $\pm 0.0284$	0.0318 $\pm 0.0008$	<b>0.0531</b> $\pm 0.004$



- GeoSim is the best model w.r.t.  $f(r_i)$  but cannot reproduce  $V_l$
- STS-EPR is better than DITRAS w.r.t. both  $f(r_i)$  and  $V_l$ : the inclusion of the sociality produces better trajectories

# Results

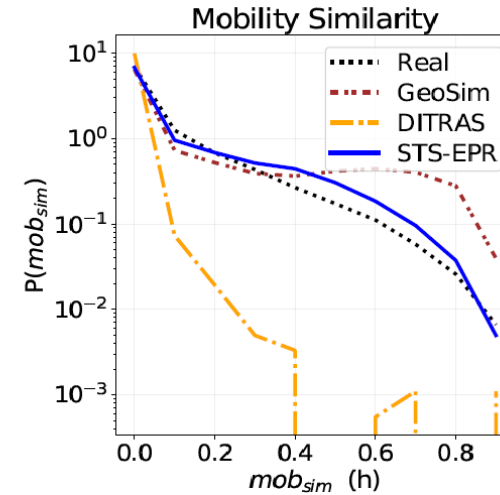
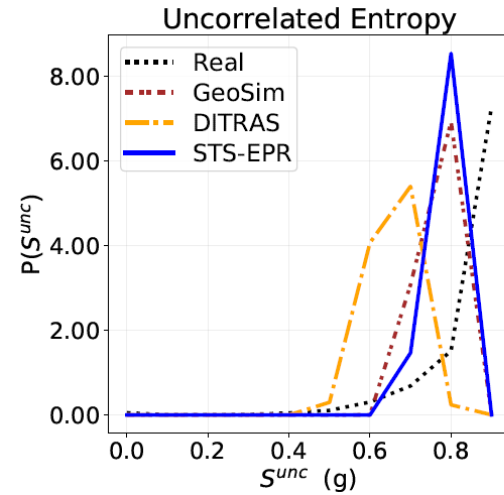


- The temporal measures are better captured by STS-EPR and DITRAS thanks to the MDG.

$\Delta_t$	$t(h)$	$E_{unc}$	$mob_{sim}$
0.1962 $\pm 0.0043$	0.281 $\pm 0.0003$	8.5182 $\pm 0.0003$	0.6097 $\pm 0.0079$
0.166 $\pm 0.0031$	0.0119 $\pm 0.0004$	3.8816 $\pm 0.1897$	0.4347 $\pm 0.0516$
<b>0.1626</b> <b><math>\pm 0.0035</math></b>	<b>0.0116</b> <b><math>\pm 0.001</math></b>	<b>2.6749</b> <b><math>\pm 0.1169</math></b>	<b>0.2543</b> <b><math>\pm 0.01</math></b>
0.2354 $\pm 0.0003$	0.2837 $\pm 0.0006$	7.1242 $\pm 0.0593$	0.0931 $\pm 0.0017$
0.2007 $\pm 0.003$	<b>0.0074</b> <b><math>\pm 0.0001</math></b>	5.0034 $\pm 0.2708$	0.923 $\pm 0.0375$
<b>0.2001</b> <b><math>\pm 0.0024</math></b>	0.0076 $\pm 0.0001$	<b>4.8717</b> <b><math>\pm 0.2247</math></b>	<b>0.014</b> <b><math>\pm 0.0009</math></b>
0.1973 $\pm 0.0004$	0.18 $\pm 0.0005$	8.0483 $\pm 0.0579$	0.5879 $\pm 0.0149$
<b>0.1665</b> <b><math>\pm 0.0032</math></b>	<b>0.0066</b> <b><math>\pm 0.0003</math></b>	<b>4.8881</b> <b><math>\pm 0.0248</math></b>	0.5425 $\pm 0.038$
0.1705 $\pm 0.0047$	0.0071 $\pm 0.0005$	5.028 $\pm 1.1511$	<b>0.3066</b> <b><math>\pm 0.0044</math></b>

# Results

	Model	$\Delta r$
London	GeoSim	0.5036 $\pm 0.0075$
	DITRAS	0.0221 $\pm 0.0022$
	<b>STS-EPR</b>	<b>0.0108</b> <b><math>\pm 0.0016</math></b>
Tokyo	GeoSim	0.7257 $\pm 0.002$
	DITRAS	0.0628 $\pm 0.0025$
	<b>STS-EPR</b>	<b>0.0485</b> <b><math>\pm 0.0013</math></b>
New York City	GeoSim	0.5947 $\pm 0.0062$
	DITRAS	<b>0.0091</b> <b><math>\pm 0.0006</math></b>
	STS-EPR	0.0188 $\pm 0.0015$



- STS-EPR is able to capture the social aspect of mobility better than GeoSim and DITRAS
- None of the presented models can replicate the distribution of  $E_{unc}$

$E_{unc}$	$mob_{sim}$
8.5182 $\pm 0.0003$	0.6097 $\pm 0.0079$
3.8816 $\pm 0.1897$	0.4347 $\pm 0.0516$
<b>2.6749</b> <b><math>\pm 0.1169</math></b>	<b>0.2543</b> <b><math>\pm 0.01</math></b>
7.1242 $\pm 0.0593$	0.0931 $\pm 0.0017$
5.0034 $\pm 0.2708$	0.923 $\pm 0.0375$
<b>4.8717</b> <b><math>\pm 0.2247</math></b>	<b>0.014</b> <b><math>\pm 0.0009</math></b>
8.0483 $\pm 0.0579$	0.5879 $\pm 0.0149$
<b>4.8881</b> <b><math>\pm 0.0248</math></b>	0.5425 $\pm 0.038$
5.028 $\pm 1.1511$	<b>0.3066</b> <b><math>\pm 0.0044</math></b>

# Open Source



```
1 from skmob.models import sts_epr
2
3 STS_epr = sts.STS_epr()
4
5 start = pandas.to_datetime('22-03-2021')
6 end = pandas.to_datetime('25-03-2021')
7 social_graph, spatial_tessellation, diary = load_parameters()
8
9 syn_trajectories = STS_epr.generate(start, end, social_graph = social_graph,
10                                     spatial_tessellation = spatial_tessellation,
11                                     diary_generator = diary)
```

<https://github.com/scikit-mobility>

# Conclusions

- STS-EPR can generate **realistic** trajectories for all the **three dimensions**, improving the state-of-the-art models GeoSim and DITRAS
- The inclusion of the social dimension in STS-EPR help improving the realism with respect to the spatial and temporal measures.
- The model can be applied to **different geographic regions** without loss of generative capability.



# Future directions

- Use of Deep Learning methods (e.g., GANs)
- External/Ausiliar information
- Include a dynamic social graph





THANKS FOR THE  
ATTENTION!



[giuliano.cornacchia@phd.unipi.it](mailto:giuliano.cornacchia@phd.unipi.it)



<https://github.com/GiulianoCornacchia>

# References

- [1] Brockmann, D., Hufnagel, L., Geisel, T., 2006. The scaling laws of human travel. *Nature* 439, 462–5.
- [2] Gonzalez, M.C., Hidalgo, C., Barabasi, A.L., 2008. Understanding individual human mobility patterns. *Nature* 453, 779–82.
- [3] Barbosa-Filho, H., Barthelemy, M., Ghoshal, G., James, C., Lenormand, M., Louail, T., Menezes, R., Ramasco, J.J., Simini, F., Tomasini, M., 2018. Human mobility: Models and applications.
- [4] Montjoye, Y.A., Hidalgo, C., Verleysen, M., Blondel, V., 2013. Unique in the crowd: The privacy bounds of human mobility. *Scientific reports* 3, 1376.
- [5] Toole, J., Herrera-Yague, C., Schneider, C., Gonzalez, M.C., 2015. Coupling human mobility and social ties. *Journal of the Royal Society, Interface / the Royal Society* 12.
- [6] Pappalardo, L., Simini, F., 2017. Data-driven generation of spatio-temporal routines in human mobility. *Data Mining and Knowledge Discovery*, 32.
- [7] Yang, D., Qu, B., Yang, J., Cudre-Mauroux, P., 2019. Revisiting user mobility and social relationships in lbsns: A hypergraph embedding approach, pp. 2147–2157
- [8] Cho, E., Myers, S., Leskovec, J., 2011. Friendship and mobility: User movement in location-based social networks, pp. 1082–1090.